

The definition of "model"

(Oxford Advanced Learners' Dictionary)

SMALL COPY

1a copy of sth, usually smaller than the original object: a working model (= one in which the parts move) of a fire engine / a model aeroplane / The architect had produced a scale model of the proposed shopping complex.

DESIGN

2a particular design or type of product: The latest models will be on display at the motor show.

DESCRIPTION OF SYSTEM

3a simple description of a system, used for explaining how sth works or calculating what might happen, etc.: a mathematical model for determining the safe level of pesticides in food

EXAMPLE TO COPY

4 something such as a system that can be copied by other people: The nation's constitution provided a model that other countries followed.

5 (approving) a person or thing that is considered an excellent example of sth: It was a model of clarity. / a model student / a model farm (= one that has been specially designed to work well)—see also role model

FASHION

6a person whose job is to wear and show new styles of clothes and be photographed wearing them: a fashion model / a male model

FOR ARTIST

7a person who is employed to be painted, drawn, photographed, etc. by an artist or photographer

(Scientific meaning)

Some sort of **simplified representations of reality** where some aspects of the truth are omitted or assumed to be unchanging so that other aspects can be observed more clearly. => classifiable to 2 groups (normative models and descriptive models)

Normative models have been used since long time ago, but descriptive models have become popular since 1950s. The oldest and most widely used normative models uses "synthetic cohort" like TFR, life table, NRR, stable population models.

Descriptive models are used for quite different purposes in demography. (1) Smoothing data (e.g., raw ASDRs may be irregular due to age-heaping or small sample sizes, so that smoothing can produce better estimates), (2) Fitting models to raw data for assessing data quality, (3) Imputing missing values or interpolating rough data (often used by historical demographers), (4) Forecasting (projecting) fertility, mortality, migrations in the future, (5) describing briefly the feature of a population (e.g., overall mortality levels can be described as life expectancy at birth using life table), (6) Evaluating the effect of changes in the determinants of mortality, fertility, and migration (e.g., Effect of rising ages at marriage or increasing contraceptive availability on fertility).

MODEL OF AGE STRUCTURE

Stable population (安定人口), Stationary population (静止人口), Intrinsic Rate of Natural Increase (内的自然増加率), Stable age distribution (安定人口分布) are the first target.

- Stable population theory, the findings by Euler (1760) and Lotka (1907): *If, in any population, mortality and fertility remain constant for a long period, and if there is no migration, then eventually a fixed age structure will develop and this "stable" age structure is completely independent from initial age structure;* where "stable" means the unchanging shape of an age distribution (total size of population is changeable).
- Special case of stable population, when growth rate is zero, is "stationary" population. The ${}_nL_x$ column in the life table is an example of stationary population.
- The size of the population consisting ${}_nL_x$ is T_0 . ℓ_0 babies are born each year. Exactly same number dies because the size of population is unchangeable. CBR in the stationary population is "Intrinsic Birth Rate" (IBR): $IBR = \ell_0/T_0$. It's exactly same as "Intrinsic Death Rate" (IDR).
- In non-stationary stable populations, $IBR \neq IDR$. The difference ($IBR - IDR$) is "Intrinsic Rate of Natural Increase" (a.k.a. "True Rate of Natural Increase" or "Lotka's r "). Age structure is unchangeable and population growth rate is r , so that every age group must be growing at the same rate of r .
- NRR is average number of daughters a woman would have if she was to experience the given mortality and fertility rates: interpreted as a measure of the extent to which the population increases in a generation. If the mean length of generation, T , is known, $NRR = \exp(rT)$. When we take logarithm of both side of the equation, $\ln(NRR) = rT$, thus $r = \ln(NRR)/T$.
- There is no simple way to calculate T , but it can be approximated by the mean age of childbearing μ , so

that $r = \ln(\text{NRR})/\mu$.

- r is quite different from CRNI (Crude Rate of Natural Increase = CBR–CDR).
- When r is positive, births in earlier years are fewer than now. The people aged 5 in 1974 is the survivors of the births of 1969.

The process of calculation in Table 11.1

ℓ_x for females and males, exact age x , number of years for each age group n , average age y , and M85+ (open-ended age groups' age-specific death rate) must be given as data.

1. Calculate the stationary population ${}_nL_x$ in normal way.
2. Calculate the intrinsic rate of natural increase, r .
3. Compute a column of the factors $\exp(-ry)$.
4. Multiply the stationary population by the factors to generate stable population.
5. The stable population is usually scaled to total population size as 10000.

Doubling time

When considering the rate of increase, it's an important question how long it would take for the population to be doubled, if the current increase rate were to continue.

If D is the doubling time and P is the population, then the population will increase exponentially to $2P$ by the formula, $2P = P \cdot \exp(-rD)$. Thus, $D = \ln(2)/r$.

* Please try Exercises 1-4.

See the R code given as <http://minato.sip21c.org/demography-special/Chap11.R>